

CRM08

Rev 1.10

BS

11/03/22

### CONTINUOUS INTERNAL EVALUATION - 3

Dept:BS	Sem / Div: III/A&B	Sub: Transform Calculus, Fourier Series and Numerical Techniques	S Code: 18MAT31
Date: 16/03/2022	Time: 9:30-11:00 am	Max Marks: 50	Elective: N

Note: Answer any 2 full questions, choosing one full question from each part.

QN	Questions	Marks	RBT	CO's
<b>PART A</b>				
1 a	Using Taylor's series Method, find the solution at $x=0.1$ of $\frac{dy}{dx} = x - y^2$ , $y(0)=1$ considering upto fourth degree term	8	L2	CO4
b	Solve $\frac{dy}{dx} = x +  \sqrt{y} $ , $y(0)=1$ at $x=0.4$ by taking $h=0.2$ using Modified Euler's Method, carry out two iterations in each step.	8	L2	CO4
c	Apply Milne's Predictor corrector formula to compute $y(2.0)$ given $\frac{dy}{dx} = \frac{1}{2}(x+y)$ with $y(0)=2$ , $y(0.5)=2.6360$ , $y(1.0)=3.5950$ , $y(1.5)=4.9680$	9	L2	CO4
<b>OR</b>				
2 a	Use Modified Euler's Method to compute $y(0.1)$ , given that $\frac{dy}{dx} = x^2 + y$ , $y(0)=1$ by taking $h=0.05$ . Perform two approximations in each step.	8	L2	CO4
b	Use Runge Kutta Method of fourth order to solve	8	L2	CO4

	$(x+y)\frac{dy}{dx}=1, y(0.4)=1$ to find $y(0.5)$ take as $h=0.1$			
c	Given $y' = x^2(1+y)$ , $y(1)=1$ , $y(1.1)=1.2330$ , $y(1.2)=1.5480$ , $y(1.3)=1.9790$ , Find $y(1.4)$ using Adam's Bashforth Method	9	L2	CO4

**PART B**

3 a	Find the curve on which the functional $\int_0^1 [(y')^2 + 12xy] dx$ can be extremised with $y(0)=0$ , $y(1)=1$	8	L3	CO5															
b	Apply Milne's Predictor Corrector Method to compute $\frac{d^2 y}{dx^2} = 1 + \frac{dy}{dx}$ at $y(0.4)$ with the initial values in table.	8	L2	CO4															
	<table border="1"> <tr> <td>x</td> <td>0</td> <td>0.1</td> <td>0.2</td> <td>0.3</td> </tr> <tr> <td>y</td> <td>1</td> <td>1.1103</td> <td>1.2427</td> <td>1.3990</td> </tr> <tr> <td>y'</td> <td>1</td> <td>1.2103</td> <td>1.4427</td> <td>1.6990</td> </tr> </table>	x	0	0.1	0.2	0.3	y	1	1.1103	1.2427	1.3990	y'	1	1.2103	1.4427	1.6990			
x	0	0.1	0.2	0.3															
y	1	1.1103	1.2427	1.3990															
y'	1	1.2103	1.4427	1.6990															
c	Prove that geodesics of a plane surface are straight lines.	9	L3	CO5															

**OR**

4 a	Find the extremal of the functional $\int_{x_1}^{x_2} [(y')^2 + y^2 + 2ye^x] dx$	8	L3	CO5
b	Given $y'' - xy' - y = 0$ with the initial conditions $y(0)=1$ and $y'(0)=0$ . Compute $y(0.2)$ using Runge Kutta Method.	8	L2	CO4
c	Derive Euler's equation in the standard form $\frac{\partial f}{\partial y} - \frac{d}{dx} \left[ \frac{\partial f}{\partial y'} \right] = 0$	9	L3	CO5

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